06_Class_Activity

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In class activity 7:

Introduction

This document demonstrates statistical analysis of lake trout mass data from Island Lake and NE 12, focusing on:

- 1. Testing assumptions for parametric tests
- 2. Transforming data when assumptions aren't met
- 3. Running different types of tests:
 - · Standard t-test
 - Log-transformed t-test
 - Welch's t-test
 - Mann-Whitney Wilcoxon test
 - · Permutation test
- 4. Interpreting and reporting results properly

What did we do last time in activity 6?

- · Assumptions of parametric tests
- alpha and beta errors
- power
- · making plots of mean and standard error

Lets start by ecploring only lake NE 12 as if you were doing a single sample T test. We will test the assumptions and then do the a T Test on NE 12 compared to Island Lake.

Part 1: Single Sample T-Test

We want to test if the mass of lake trout differ in NE 12 from a mean of 500g.

Activity: Define hypotheses and identify assumptions

- H_0 : $\mu = 500$ (The mean mass of lake trout in NE12 is 500 g)
- H_1 : $\mu \neq 500$ (The mean mass of lake trout in NE12 is not 500 g)

Assumptions for t-test:

- 1. Data is normally distributed
- 2. Observations are independent
- 3. No significant outliers

Part 1: Load Data and Test Assumptions

First we need to load the data for all the lakes and we can look at what we have...

How may lakes are there?

```
# Install packages if needed (uncomment if necessary)
# install.packages("readr")
```

```
# install.packages("tidyverse")
# install.packages("car")
# install.packages("here")

# Load required packages
library(tidyverse) # For data manipulation and visualization
library(car) # For statistical tests
library(patchwork) # For combining plots
library(perm) # For permutation tests
```

```
# Load the pine needle data
# Use here() function to specify the path
# Read in the lake trout data
lt_df <- read_csv("data/lake_trout.csv")</pre>
```

```
Rows: 1502 Columns: 5

— Column specification

Delimiter: ","

chr (3): sampling_site, species, lake

dbl (2): length_mm, mass_g

i Use `spec()` to retrieve the full column specification for this data.

i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

```
# Examine the first few rows
head(lt_df)
```

Part 1: Exploratory Data Analysis

Before conducting hypothesis tests, we should always explore our data to understand its characteristics.

Let's calculate summary statistics and create visualizations.

Activity: Calculate basic summary statistics for lake trout mass

```
# YOUR TASK: Calculate summary statistics for lake trout mass
# Hint: Use summarize() function to calculate mean, sd, n, etc.

# Create a summary table for all lake trout

df_summary <- lt_df %>%
    # group_by(lake) %>%
    summarize(
    mean_length = mean(length_mm, na.rm=TRUE),
```

```
sd_length = sd(length_mm, na.rm=TRUE),
n = sum(!is.na(length_mm)),
se_length = sd_length / sqrt(n)
)
print(df_summary)
```

```
# Now calculate summary statistics by lake
# YOUR CODE HERE
```

Create a New dataframe of lake NE12 only

```
# add your code here
nel2_df <- lt_df %>%
filter(lake == "NE 12") %>%
filter(!is.na(mass_g)) # Remove any NA values
```

Part 1: Testing Assumptions

Before conducting our t-test, we need to verify that our data meets the necessary assumptions.

Activity: Test the normality assumption

Methods to test normality:

- Visual methods:
 - QQ plots or histograms
 - ► Statistical tests: Shapiro
 - ▶ Wilk test

Part 1: Visualizing the assumptions and data

Activity: Create visualizations of lake trout mass

Create a histogram and a boxplot to visualize the distribution of lake trout massvalues.

Effective data visualization helps us understand:

- The central tendency
- The spread of the data
- Potential outliers
- Shape of distribution

Your Task

```
# YOUR TASK: Create a histogram of lake trout mass
# Hint: Use ggplot() and geom_histogram()
# Histogram of all lake trout weights
```

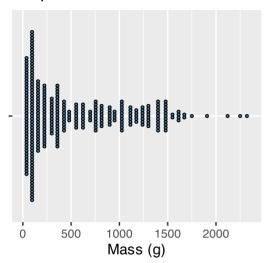
```
75 - 100 50 - 1000 1500 2000 2500 mass (g)
```

```
# how can you make a dataframe only for lake NE 12
# and
# make a histogram for lake NE 12
# Note we need the dataframe to make life a bit easier
```

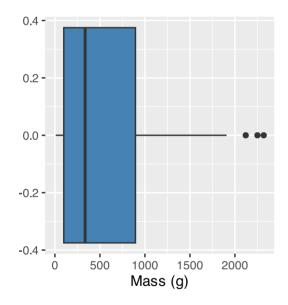
Now to make the various plots we talk about only for lake NE 12

```
# 2. Dotplot
ne12_dot_plot <- ggplot(ne12_df, aes(x = mass_g, y = "")) +
  geom_dotplot(binwidth = 60, stackdir = "center", fill = "steelblue", dotsize = 0.5) +
  labs(title = "Dotplot", x = "Mass (g)", y = "")
ne12_dot_plot</pre>
```

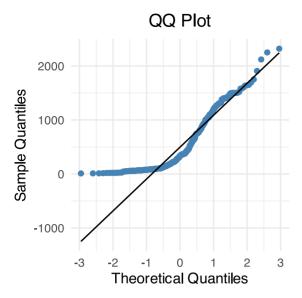
Dotplot



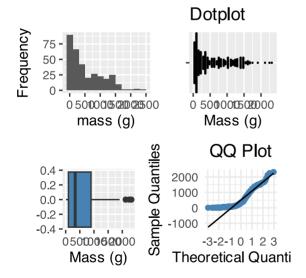
```
# 3. Boxplot
nel2_box_plot <- ggplot(nel2_df, aes(y = mass_g)) +
    geom_boxplot(fill = "steelblue") +
    labs( y = "Mass (g)", x = "") +
    coord_flip()
nel2_box_plot</pre>
```



```
nel2_qq_plot <- ggplot(nel2_df, aes(sample = mass_g)) +
    stat_qq(color = "steelblue") +
    stat_qq_line() +
    labs(title = "QQ Plot", x = "Theoretical Quantiles", y = "Sample Quantiles") +
    theme_minimal() +
    theme(plot.title = element_text(hjust = 0.5))
nel2_qq_plot</pre>
```



Use Patchwork to combine the plots



Shapiro-Wilk's Test

Really want to do this on residuals

```
# Shapiro-Wilk test
shapiro_test <- shapiro.test(ne12_df$mass_g)
print(shapiro_test)</pre>
```

```
Shapiro-Wilk normality test

data: ne12_df$mass_g
W = 0.85148, p-value < 2.2e-16
```

Now that we show how mass of lake NE 12 fails what do we do next?

Lets explore a comparison of NE 12 and Island Lake mass g

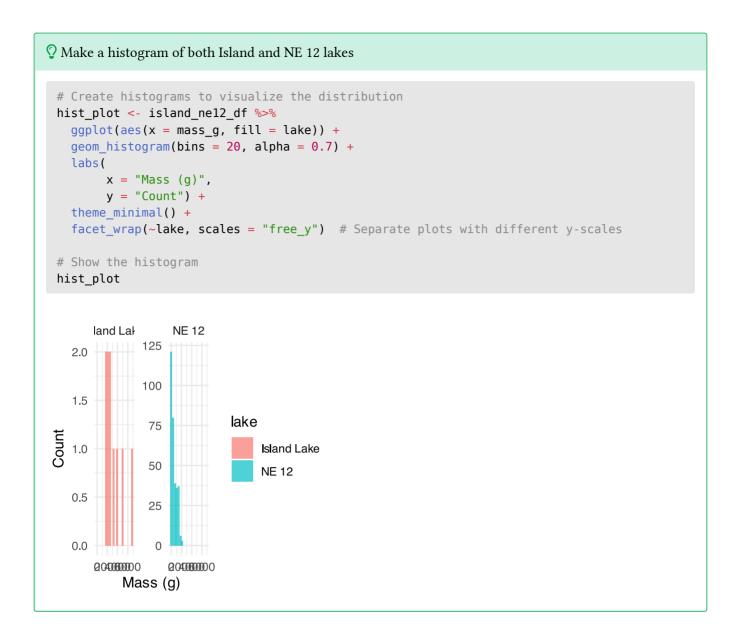
```
© Exercise: Create a island_ne12_df dataframe from
We could also look at the difference in means... some cool code here
 # Create a dataframe with just Island Lake and NE 12 lakes
 # Filter out any NA values for mass
 island_ne12_df <- lt_df %>%
   filter(lake %in% c("NE 12", "Island Lake")) %>%
   filter(!is.na(mass q))
 # Look at the first few rows
 head(island_ne12_df)
 # A tibble: 6 \times 5
   sampling_site species
                           length_mm mass_g lake
               <chr>
                                <dbl> <dbl> <chr>
   <chr>
 1 Island Lake lake trout
                                  640
                                       2600 Island Lake
 2 Island Lake lake trout
                                  650
                                       2350 Island Lake
 3 Island Lake lake trout
                                  585
                                       2200 Island Lake
 4 Island Lake lake trout
                                        3950 Island Lake
                                  720
 5 Island Lake lake trout
                                        6800 Island Lake
                                  880
 6 Island Lake lake trout
                                  830
                                        3200 Island Lake
```

© Get summary stats for lake trout mass in NE12 and Island lakes

Get a summary of the data by lake

```
# Get a summary of the data by lake
summary_by_lake <- island_ne12_df %>%
  group_by(lake) %>%
  summarise(
                                          # Count of observations
    n = n()
    m = n(),
mean_mass = mean(mass_g),
sd_mass = sd(mass_g),
se_mass = sd_mass / sqrt(n),
# Count of observation
# Mean mass
# Standard deviation
# Standard error
    min_mass = min(mass_g),  # Minimum mass
max_mass = max(mass_g)  # Maximum mass
# View the summary
summary_by_lake
# A tibble: 2 \times 7
  lake
               n mean_mass sd_mass se_mass min_mass max_mass
  <chr>
               <int>
                             <dbl>
                                       <dbl>
                                                <dbl>
                                                                       <dbl>
1 Island Lake 10
                             3165
                                       1617.
                                                 511.
                                                            1650
                                                                        6800
2 NE 12
                              534.
                                        520.
                                                 29.0
                                                                        2320
```

Visualize data by lake



Practice for later if you choose

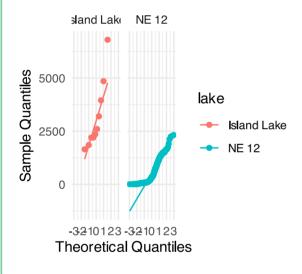
Informal Normality test - often better

© Exercise: check normality

Always do a qq plot

In a QQ plot, points that follow the line indicate data that follows a normal distribution. Deviations from the line suggest non-normality.

QQ Plot for Normality Check



Formal normality test

© Exercise: do a Shapiro-Wilk Test

We can do a formal test for a p value

Note island looks non normal in the qqplot but its really close with the Shapiro-Wilk test...

```
# Formal test for normality: Shapiro-Wilk test
# We'll do this for each lake separately
# For NE 12
ne12_data <- island_ne12_df %>%
 filter(lake == "NE 12") %>%
  pull(mass_g)
# For Island Lake
island data <- island ne12 df %>%
  filter(lake == "Island Lake") %>%
  pull(mass q)
# Run Shapiro-Wilk test
shapiro_ne12 <- shapiro.test(ne12_data)</pre>
shapiro_island <- shapiro.test(island_data)</pre>
# Show results
cat("Shapiro-Wilk normality test for NE 12:\n")
Shapiro-Wilk normality test for NE 12:
print(shapiro_ne12)
    Shapiro-Wilk normality test
data: ne12_data
W = 0.85148, p-value < 2.2e-16
cat("\nShapiro-Wilk normality test for Island Lake:\n")
Shapiro-Wilk normality test for Island Lake:
print(shapiro_island)
    Shapiro-Wilk normality test
data: island_data
W = 0.84102, p-value = 0.04538
```

© Exercise: test for equal variances

Again we want the P value not significant

The Levene's test has the following null hypothesis: - H_0 : The variances are equal across groups - H_1 : The variances are not equal across groups

If the p-value is less than 0.05, we reject the null hypothesis and conclude the variances are not equal.

Transformations

Commonly a log10 transformation works well.

© Exercise: do a log transformation of Log 10

We could also look at the difference in means... some cool code here

```
# Add log-transformed mass variable to our dataset
island ne12 df <- island ne12 df %>%
  mutate(log mass = log10(mass g)) # Create log10 transformed mass
head(island_ne12_df)
# A tibble: 6 \times 6
  1 Island Lake lake trout 640 2600 Island Lake
2 Island Lake lake trout 650 2350 Island Lake
3 Island Lake lake trout 585 2200 Island Lake
4 Island Lake lake trout 720 3950 Island Lake
5 Island Lake lake trout 880 6800 Island Lake
6 Island Lake lake trout 830 3200 Island Lake
                                                                              3.41
                                                                             3.37
                                                                             3.34
                                                   3950 Island Lake 3.60
                                                    6800 Island Lake 3.83
6 Island Lake lake trout
                                           830
                                                   3200 Island Lake
                                                                             3.51
```

Now look at histograms of logged data

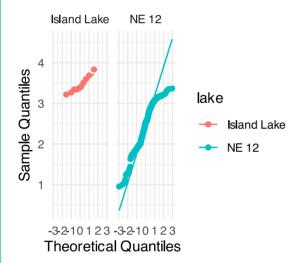
© Exercise: histogram of transformed data We need to see if it worked # Create histograms of log-transformed data log_hist_plot <- island_ne12_df %>% ggplot(aes(x = log mass, fill = lake)) +geom_histogram(bins = 20, alpha = 0.7) + labs(title = "Distribution of Log-Transformed Lake Trout Mass", x = "Log10 Mass",y = "Count") +theme minimal() + facet_wrap(~lake, scales = "free_y") # Show the log-transformed histogram log_hist_plot Distribution of Log-Transformed sland Lake NE 12 40 30 lake 20 Island Lake NE 12 10 0 1 2 3 4 1 2 3 4 Log10 Mass

Now a qqplot - we will skip Shapiro-Wilk this time;)

© Exercise: do a qqplot of transformed data

We could also look at the difference in means... some cool code here

QQ Plot for Log-Transformed Da



© Exercise: Shapiro-Wilk test

```
# Check normality of log-transformed data using Shapiro-Wilk test
# For NE 12
log_ne12 <- island_ne12_df %>%
  filter(lake == "NE 12") %>%
  pull(log mass)
# For Island Lake
log_island <- island_ne12_df %>%
  filter(lake == "Island Lake") %>%
  pull(log_mass)
# Run Shapiro-Wilk test on log-transformed data
shapiro_log_ne12 <- shapiro.test(log_ne12)</pre>
shapiro log island <- shapiro.test(log island)</pre>
# Show results
cat("Shapiro-Wilk normality test for log-transformed NE 12 data:\n")
Shapiro-Wilk normality test for log-transformed NE 12 data:
print(shapiro_log_ne12)
    Shapiro-Wilk normality test
data: log_ne12
W = 0.95384, p-value = 1.583e-08
cat("\nShapiro-Wilk normality test for log-transformed Island Lake data:\n")
Shapiro-Wilk normality test for log-transformed Island Lake data:
print(shapiro_log_island)
    Shapiro-Wilk normality test
data: log island
W = 0.93396, p-value = 0.4879
```

Transformation fails! What next

For grins lets do the Two Sample T Test anyway

```
🗘 Exercise: Two sample T Test on regular data
Try a t test
 # Run a standard two-sample t-test
 t_test_result <- t.test(</pre>
   mass_g ~ lake,
   data = island_ne12_df,
   var.equal = TRUE, # Assumes equal variances
   alternative = "two.sided"
 # Show the results
 print(t test result)
     Two Sample t-test
 data: mass_g by lake
 t = 14.181, df = 330, p-value < 2.2e-16
 alternative hypothesis: true difference in means between group Island Lake and group NE
 12 is not equal to 0
 95 percent confidence interval:
  2266.304 2996.360
 sample estimates:
 mean in group Island Lake mean in group NE 12
                 3165.0000
                                             533.6677
```

© Exercise: Two sample T Test on transformed data

Try a t test

```
# Run a t-test on log-transformed data
log_t_test_result <- t.test(
    log_mass ~ lake,
    data = island_ne12_df,
    var.equal = TRUE, # Assumes equal variances
    alternative = "two.sided"
)

# Show the results
print(log_t_test_result)</pre>
```

© Exercise: Looking at results of log10 data

When analyzing log-transformed data:

- 1. The mean of log-transformed data, when back-transformed, gives the geometric mean (not the arithmetic mean)
- 2. The back-transformed confidence intervals represent the confidence interval for the geometric mean
- 3. Report results like: "The geometric mean mass of lake trout in NE 12 was X g (95% CI: Y-Z)"
- 4. Note you can't take the 10^SE to get the standard errors but rather you need to get the mean seand the mean + se and then backtransform...

```
# Calculate back-transformed means and confidence intervals
# This converts log values back to original scale
back_transformed <- island_ne12_df %>%
  group by(lake) %>%
  summarise(
    n = n()
    mean_log = mean(log_mass),
    sd log = sd(log mass),
    se_log = sd_log / sqrt(n),
    # Back-transform mean
    geometric_mean = 10^mean_log,
    # Back transform SE
    lower se = 10^{\text{mean log -se log}},
    upper_se = 10^(mean_log + se_log),
    # Back-transform confidence intervals (approximate method)
    lower_ci = 10^(mean_log - qt(0.975, n-1) * se_log),
    upper ci = 10^{(mean log + qt(0.975, n-1))} * se log)
# Show back-transformed results
print(back transformed)
# A tibble: 2 \times 10
              n mean_log sd_log se_log geometric_mean lower_se upper_se lower_ci
  <chr>
          <int>
                   <dbl> <dbl> <dbl>
                                                 <dbl>
                                                           <dbl>
                                                                    <dbl>
                                                                             <dbl>
1 Island...
             10
                    3.46 0.195 0.0618
                                                 2868.
                                                           2487.
                                                                    3307.
                                                                             2078.
                                                            268.
                                                                     308.
2 NE 12
            322
                    2.46 0.541 0.0302
                                                  287.
                                                                              251.
# i 1 more variable: upper_ci <dbl>
```

Now plot the back transformed data

In some cases the error bars are not symmetrical

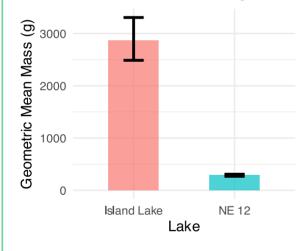
② Exercise:

Try

```
# Create a plot showing geometric means with SE bars
geo_mean_plot <- back_transformed %>%
  qqplot(aes(x = lake, y = qeometric mean, fill = lake)) +
  # Add bars for geometric means
  geom_bar(stat = "identity", width = 0.5, alpha = 0.7) +
  # Add error bars for standard error
  geom errorbar(aes(ymin = lower se, ymax = upper se),
                width = 0.2, linewidth = 1) +
  # Add labels and title
  labs(title = "Geometric Mean Lake Trout Mass with Standard Error",
       subtitle = "Back-transformed from log10 scale",
       x = "Lake",
       y = "Geometric Mean Mass (g)") +
  # Use a clean theme
  theme minimal() +
  # Remove legend (since we already have lake on x-axis)
  theme(legend.position = "none")
# Display the plot
geo mean plot
```

Geometric Mean Lake Trout N

Back-transformed from log10 scale



3. Welch's t-test

```
# Run Welch's t-test (doesn't assume equal variances)
welch_test_result <- t.test(
  mass_g ~ lake,
  data = island_ne12_df,
  var.equal = FALSE, # Does NOT assume equal variances
  alternative = "two.sided"
)</pre>
```

```
# Show the results
print(welch_test_result)
```

♥ When to Use Welch's t-test

Welch's t-test is preferred when:

- - Group variances are unequal (as indicated by Levene's test)
- - Sample sizes are different between groups
- - It's more robust than the standard t-test in many situations

4. Mann-Whitney Wilcoxon test

```
# Run Mann-Whitney U test (non-parametric alternative to t-test)
wilcox_test_result <- wilcox.test(
  mass_g ~ lake,
  data = island_ne12_df,
  alternative = "two.sided"
)

# Show the results
print(wilcox_test_result)</pre>
```

```
Wilcoxon rank sum test with continuity correction

data: mass_g by lake

W = 3205.5, p-value = 9.506e-08

alternative hypothesis: true location shift is not equal to 0
```

When to Use Mann-Whitney Wilcoxon Test

This non-parametric test is preferred when:

- - Data is not normally distributed (even after transformation)
- - Comparing medians rather than means
- - Data contains outliers that might affect a t-test
- - It compares the ranks of the values rather than the actual values

5. Permutation test

```
# First, let's make sure we have balanced samples
# We'll select a random subset from NE 12 to match Island Lake size
set.seed(123) # For reproducibility
# Get the smaller sample size
island size <- sum(island ne12 df$lake == "Island Lake")</pre>
# Randomly sample from NE 12 to match Island Lake size
ne12 sample <- island ne12 df %>%
 filter(lake == "NE 12") %>%
 slice_sample(n = island_size)
# Combine with Island Lake data
balanced df <- bind rows(</pre>
  ne12_sample,
  island ne12 df %>% filter(lake == "Island Lake")
)
# Extract mass data by lake
ne12 mass <- balanced df %>%
  filter(lake == "NE 12") %>%
  pull(mass_g)
island_mass <- balanced_df %>%
  filter(lake == "Island Lake") %>%
  pull(mass_g)
# Run permutation test
perm test result <- permTS(</pre>
 x = ne12 mass,
  y = island_mass,
  alternative = "two.sided",
  method = "exact.mc", # Monte Carlo method for large samples
  control = permControl(nmc = 10000) # Number of Monte Carlo replications
)
# Show the results
print(perm_test_result)
```

When to Use Permutation Tests

Permutation tests are useful when:

- - Sample sizes are small
- - Data doesn't meet the assumptions for parametric tests
- - You want a robust test that makes minimal assumptions about the data
- - They can test any statistic, not just means

Now lets compare all of the results

Let's compare the results from all tests:

```
# Create a summary table of test statistics and p-values
test results <- data.frame(</pre>
 Test = c("Standard t-test",
           "Log-transformed t-test",
           "Welch's t-test",
           "Mann-Whitney Wilcoxon test"),
  Statistic = c(paste("t =", round(t_test_result$statistic, 2)),
               paste("t =", round(log t test result$statistic, 2)),
               paste("t =", round(welch_test_result$statistic, 2)),
               paste("W =", wilcox test result$statistic)),
  p_value = c(t_test_result$p.value,
             log t test result$p.value,
             welch_test_result$p.value,
             wilcox test result$p.value),
  Significant = c(t test result p.value < 0.05,
                 log_t_test_result$p.value < 0.05,</pre>
                 welch_test_result$p.value < 0.05,</pre>
                 wilcox test result$p.value < 0.05)</pre>
)
# Display the results
test_results
```

```
Test Statistic p_value Significant

1 Standard t-test t = 14.18 \cdot 5.667524e-36 TRUE

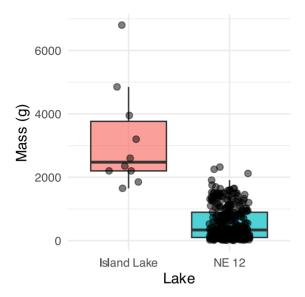
2 Log-transformed t-test t = 5.82 \cdot 1.399864e-08 TRUE

3 Welch's t-test t = 5.14 \cdot 6.016186e-04 TRUE

4 Mann-Whitney Wilcoxon test W = 3205.5 \cdot 9.506478e-08 TRUE
```

Visualizing Results

Show the plot
combined_plot



When reporting results from statistical tests, include:

For Standard t-test:

Lake trout from NE 12 had significantly different mass (M = [mean], SD = [SD]) compared to Island Lake (M = [mean], SD = [SD]), t([df]) = [t-value], p = [p-value].

For Log-transformed t-test:

After log transformation to meet normality assumptions, lake trout from NE 12 had significantly different mass (geometric mean = [value], 95% CI [lower-upper]) compared to Island Lake (geometric mean = [value], 95% CI [lower-upper]), t([df]) = [t-value], p = [p-value].

For Welch's t-test:

Assuming unequal variances, lake trout from NE 12 had significantly different mass (M = [mean], SD = [SD]) compared to Island Lake (M = [mean], SD = [SD]), Welch's t([df]) = [t-value], p = [p-value].

For Mann-Whitney Wilcoxon test:

Lake trout mass differed significantly between NE 12 (Mdn = [median]) and Island Lake (Mdn = [median]), W = [W-value], p = [p-value].

For Permutation test:

Permutation testing (10,000 iterations) revealed significant differences in lake trout mass between NE 12 and Island Lake, p = [p-value].

Conclusion

This analysis demonstrates several approaches to comparing mass between lake trout populations. The choice of statistical test depends on whether your data meets the assumptions of parametric tests. When assumptions are violated:

- 1. Try transforming the data (e.g., log transformation)
- 2. Use Welch's t-test if variances are unequal
- 3. Use non-parametric tests (Mann-Whitney or permutation tests) if data remains non-normal

All methods have their strengths and limitations, and the consistency of results across methods can strengthen your conclusions.

- **Standard t-test**: When data is normally distributed with equal variances
- Log-transformed t-test: When raw data is skewed but log-transformation achieves normality
- Welch's t-test: When variances are unequal
- Mann-Whitney Wilcoxon test: When data is not normal and cannot be transformed to normality
- Permutation test: When sample sizes are small or assumptions cannot be met